

CSE 114A Final, Winter 2024

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- DO NOT TURN THIS PAGE OVER BEFORE WE TELL YOU TO
- You have **180 minutes** to complete this exam.
- Where limits are given, **write no more** than the amount specified.
- You may refer to a **double-sided cheat sheet**, but no electronic materials.
- Avoid seeing anyone else's work or allowing yours to be seen.
- Do not communicate with anyone but an exam proctor.
- If you are unsure of how to interpret a problem description, state your interpretation clearly and concisely. Reasonable interpretations will be taken into account by the graders.
- The back side of each page will not be scanned or graded, but you can use it as scratch paper if you like.
- All questions are worth equal points.
- **Good luck!**

Q1: Scope

What are the free variables of this λ -term?

$(\lambda a d \rightarrow b (\lambda b \rightarrow c a)) d$

- No free variables
- a, b, c, d
- b, c, d
- a, c, d
- a, b, d
- a, b, c
- b, c

Q2: Normal Forms

Which of the following terms are in normal form:

- x
- x y
- $(\lambda x \rightarrow x) y$
- x $(\lambda y \rightarrow y)$
- $(\lambda y \rightarrow y y) (\lambda y \rightarrow y y)$

Q3: Reductions

Evaluate this λ -term to a normal form, and for each reduction write in the appropriate blank space whether it is an $=a>$ step (α -renaming) or a $=b>$ step (β -reduction). (You do not need to use all of the blank lines below.)

$(\lambda f x \rightarrow f (f x)) (\lambda y \rightarrow x y) \text{ three}$

$= _ > _$

$= _ > _$

$= _ > _$

$= _ > _$

$= _ > _$

$= _ > _$

Q4: Haskell map and foldl

What does this Haskell expression evaluate to?

```
foldl (+) 3 (map (\(x,y) -> y+1) [(0,1), (2,3), (4,5)])
```

Answer: _____

Q5: Haskell map and foldr

What does this Haskell expression evaluate to?

```
foldr (+) 3 (map (\(x,y) -> x+1) [(0,1), (2,3), (4,5)])
```

Answer: _____

Q6: Haskell foldr

What does this Haskell expression evaluate to?

```
foldr (\(x,y) (a,b) -> (x+a,y+b)) (0,1) [(0,1), (2,3), (4,5)]
```

Answer: _____

Q7: Haskell foldl 1

In the context of the following function definition:

```
foo f = foldl (\b x -> (f x) : b) []
```

what does this Haskell expression evaluate to?

```
foo (\x -> x+1) [1,2,3]
```

Answer: _____

Q8: Haskell foldl 2

In the context of the same function definition above, what does this Haskell expression evaluate to?

```
foo (\x -> x+1) (foo (\x -> x+1) [1,2,3])
```

Answer: _____

Q9: Haskell filter

What does this Haskell expression evaluate to?

```
filter (\(x,y) -> x < y) [(even,1), (\x->x>2,3), (even,6)]
```

Answer: _____

Q10: Haskell data types

Consider the following datatype definition:

```
data Paragraph = Text String | Heading Int String | Bullets Bool [String]
```

What is the type of `Heading`?

`Heading :: _____`

Q11: Haskell data types (continued)

In the context of the above datatype definition, what is the type of

```
(\p ->  
  case p of  
    Text x -> x  
  | Heading x y -> y)
```

Answer: _____

Q12: Haskell data types (continued)

Consider the datatype below for a tree.

```
data Tree = Leaf
          | Node Int Tree Tree
```

Write a function that sums all the integer in a trees.

Your solution should not be recursive, and instead should be defined in terms of the `foldTree` function below, by passing in the correct three arguments to `foldTree`.

```
foldTree :: (Int -> Int -> Int -> Int) -> Int -> Tree -> Int
foldTree op base Leaf = base
foldTree op base (Node n l r) = op n (foldTree op base l) (foldTree op base r)
```

```
sumTree :: Tree -> Int
```

```
sumTree t = foldTree -----
```

Q13: Haskell data types (continued)

The function `foldTree` above has a more general/polymorphic type. What is it?

Answer: `foldTree :: _____`

Q14: Haskell data types (continued)

Write an instance of the type class `Show` for the datatype `Tree` according to the following examples. Pay attention to including the correct parentheses and spacing. Remember that `(++)` concatenates Strings, and `(show n)` converts an `Int n` into a String. It is ok if your code splits up over multiple lines.

```
-- Examples:  
-- show Leaf returns "Leaf"  
-- show (Node 4 Leaf Leaf) returns "(Node 4 Leaf Leaf)"  
-- show (Node 3 (Node 4 Leaf Leaf) (Node 5 Leaf Leaf))  
--   returns "(Node 3 (Node 4 Leaf Leaf) (Node 5 Leaf Leaf))"
```

instance

Q15: Implementing An Interpreter

Fill in the blanks in the following Haskell code to define an evaluator for this small programming language:

```
data Expr = Num Int
          | Add Expr Expr

eval :: Expr -> Int

eval (Num n)      = -----
eval (Add e1 e2) = -----
```

Q16: Free Variables

For the following small language, define a function `free` so that `free x e` determines if the variable `x` occurs free in the expression `e`.

```
type Id = String
data Expr = Num Int
          | Lam Id Expr
          | Var Id
          | App Expr Expr

free :: Id -> Expr -> Bool
```

Q17: Static and Dynamic Scope

Consider the following code fragment:

```
let euroToUSD = 1.1 in
let convertEurosToDollars eu = eu * euroToUSD in
let euroToUSD = 0.9 in
convertEurosToDollars 100
```

What would this code evaluate to under:

- Static (aka Lexical) Scope: _____
- Dynamic Scope: _____

Q18: Type Systems

What is the result of applying the substitution $U = [a / \text{Int}, c / \text{Int}]$ to the type $(\text{Int} \rightarrow a \rightarrow b)$

Answer: _____

Q19: Type Systems (continued)

What substitution is the most general unifier of the following two types:

- $(\text{Int} \rightarrow b)$
- $(a \rightarrow \text{Int} \rightarrow \text{Int})$

Answer: _____

Haskell Cheat Sheet

Here is a list of definitions you may find useful:

```
foldr :: (a -> b -> b) -> b -> [a] -> b
foldr f b []      = b
foldr f b (x:xs) = f x (foldr f b xs)

foldl :: (b -> a -> b) -> b -> [a] -> b
foldl f b xs      = helper b xs
  where
    helper acc []      = acc
    helper acc (x:xs) = helper (f acc x) xs

filter :: (a -> Bool) -> [a] -> [a]
filter pred []      = []
filter pred (x:xs)
  | pred x          = x : filter pred xs
  | otherwise       = filter pred xs

map :: (a -> b) -> [a] -> [b]
map _ []           = []
map f (x:xs)      = f x : map f xs

flip :: (a -> b -> c) -> b -> a -> c
flip f x y = f y x

(+++) :: [a] -> [a] -> [a]
(+++) []      ys = ys
(+++) (x:xs) ys = x : xs +++ ys

even :: (Integral a) => a -> Bool
(==) :: Eq a => a -> a -> Bool
max  :: Ord a => a -> a -> a
(<)  :: Ord a => a -> a -> Bool
(>)  :: Ord a => a -> a -> Bool
(>=) :: Ord a => a -> a -> Bool
(<=) :: Ord a => a -> a -> Bool
```