CSE114A, Fall 2024: Midterm Exam

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Student name: ____

CruzID (the part before the "@" in your UCSC email address):

Additionally, please write your CruzID at the top of each page.

This exam has 5 questions and 70 total points.

Instructions

- Please write directly on the exam.
- For multiple choice questions, fill in the letter completely, e.g. from (a) to
- For short response questions, try to keep your answer within the outlined box.
- You have 65 minutes to complete this exam. You may leave when you are finished.
- This exam is **closed book**. You may use one double-sided page of notes, but no other materials.
- Avoid seeing anyone else's work or allowing yours to be seen.
- Please, no talking. No notes, books, laptops, phones, or other electronic devices. Do not communicate with anyone but an exam proctor.
- To ensure fairness (and the appearance thereof), **proctors will not answer questions about the content of the exam**. If you are unsure of how to interpret a problem description, state your interpretation clearly and concisely. *Reasonable interpretations* will be taken into account by graders.

Good luck!

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Part 1: Lambda calculus

```
Question 1 (12 points)
   Consider the following lambda calculus expression, which we will name EXPR1
       (x y z \rightarrow ITE (OR a b) c
                             ((\w -> \text{ITE} (\text{ISZ w}) (\text{ADD x y}) w) \text{ FOUR})) ONE TWO
    1.1 (3 points) What are the free variables of EXPR1:
              (a) x, y, and z
              (b) a, b, and c
              ⓒ x, y, z, and w
              (d) Choices (b) and (c)
              (e) None of the above
    1.2 (4 points) After a single beta-reduction on EXPR1, what would the resulting expression be?:
              (a) (y z \rightarrow ITE (OR a b) c
                            ((\w -> ITE (ISZ w) (ADD ONE y) w) FOUR)) TWO
              () (x y z \rightarrow ITE (OR a b) c
                               (ITE (ISZ FOUR) (ADD x y) FOUR)) ONE TWO
              (c) (\y z -> ITE (OR a b) c
                            (ITE (ISZ FOUR) (ADD ONE y) FOUR)) TWO
              (d) Choices (a) and (b)
              (e) Choices (a) and (c)
    1.3 (5 points) What is the normal form of EXPR1:
              (a) THREE
              (b) FOUR
              (c) \ z \rightarrow (a TRUE b) c FOUR
              (d) \setminus z \rightarrow ITE (OR a b) c FOUR
              (e) None of the above
```

Question 2 (12 points)

Recall that =d> in ELSA denotes unfolding a definition. Suppose a new ELSA operator = $b\sim$ > denotes a sequence of one or more **beta-reductions** ending in an expression that cannot be beta-reduced without expanding a definition.

Reduce the following lambda expression to normal form using $=b \rightarrow and =d >$.

• Hint: =b~> is a little like =~> but can only take beta-reduction steps. Use =b~> to reduce expressions that contain a redex (the initial expression below is an example of a redex) until you reach an expression that can't be beta-reduced because the definitions haven't been expanded. Then, expand a definition with =d> and continue to beta-reduce with =b~> until you reach a normal form with no remaining definitions.

 $(\x ->$ ITE x FIVE TWO) FALSE

Part 2: Haskell

```
Question 3 (10 points)
   Consider the following Haskell expression
      let
        acc = (0, 0)
        val = [(0, 1), (2, 3), (4, 5), (6, 7), (8, 9)]
        foldx = foldr f1 acc val
        in
          foldl f2 (12,34) [foldx]
        where
          f1 (x, y) (u, w) = (x + u, y + w)
          f2 (x, y) (u, w) = (x - u, y - w)
   3.1 (5 points) What is the type of f1?
            (a) [Int] -> [Int] -> [Int]
            (Int, Int) -> (Int, Int) -> (Int, Int)
            \bigcirc Int -> Int -> (Int, Int)
            (d) None of the above
            (e) Syntax or type error
   3.2 (5 points) What is the type of foldx?
            (Int, Int)
            (b) [Int]
            (c) Int
            (d) None of the above
```

e) Syntax or type error

Question 4 (24 points)

Recall that the Fibonacci sequence is a sequence in which each number is the sum of the two preceding ones. Starting from 0 and 1, the sequence will be $0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, \cdots$

Please complete the implementation below of a function that returns the N-th number in Fibonacci sequence that starts from 0 and 1.

4.1 (3 points) Please fill in the blanks **<u>blank_1</u>** in the box below:

4.2 (3 points) Please fill in the blanks **<u>blank</u>** in the box below:

4.3 (3 points) Please fill in the blanks **blank_3** in the box below:

4.4 (5 points) Next, please complete the implementation below of the same function but using tail recursion

Please fill in the blank **<u>blank_1</u>** in the box below:

4.5 (10 points) In addition to the Fibonacci sequence, Factorial sequence is another famous number sequence. Below is the function that returns the N-th number in the Factorial sequence that starts from 0.

Now, please implement the function:

seqArray :: (Int -> Int) -> Int -> [Int]

seqArray accepts a number sequence function and an integer representing N, and returns an array of the given number sequence from 0 to the N-th number.

For example, seqArray fib 10 should returns [0,1,1,2,3,5,8,13,21,34,55] And seqArray fac 5 should returns [1,1,2,6,24,120]

Please implement seqArray using tail recursion if you can. 7 points for correct implementation, 3 points for correct tail recursive implementation, total 10 possible points.

Question 5 (12 points)

5.1 (6 points) Consider the following data type and function definition. What typeclass instances, if any, are required for the following function to typecheck? Just list names, no definitions are required.

5.2 (6 points) Consider the following function

```
sameSide :: Triangle -> Triangle -> Bool
sameSide (ASA _ y _) (ASA _ y' _) = y == y'
sameSide (SSS x y z) (ASA _ y' _) = x == y' || y == y' || z == y'
sameSide (SAS x _ z) _ = True
sameSide _ (ASA _ _ ) = False
```

What would the following expression evaluate to?

sameSide (ASA 1 2 3) (SSS 2 2 2)

- (a) True
- (b) False
- © Type error
- (d) Runtime error
- (e) None of the above

1 Lambda calculus cheat sheet

```
-- Booleans -----
let TRUE =\x y \rightarrow x
let FALSE = \langle x y \rangle \rightarrow y
let ITE = \b x y \rightarrow b x y
let NOT = \b x y \rightarrow b y x
let AND = b1 b2 \rightarrow ITE b1 b2 FALSE
let OR = b1 b2 \rightarrow ITE b1 TRUE b2
-- Numbers -----
let ZERO = \final f x-> x
let ONE = \final f x \rightarrow f x
let TWO = \langle f x - \rangle f (f x)
let THREE = \f x \rightarrow f (f (f x))
let FOUR = \langle f x \rangle - \langle f (f (f x)) \rangle
let FIVE = \langle f x \rangle \rightarrow f (f (f (f (f x))))
-- Pairs ------
let PAIR = \x y b \rightarrow b x y
let FST = \p -> p TRUE
let SND = \p -> p FALSE
-- Arithmetic -----
let INC = \n f x \rightarrow f (n f x)
let ADD = \n m \rightarrow n INC m
let MUL
         = \n m -> n (ADD m) ZERO
let ISZ = \langle n \rangle n (\langle z \rangle FALSE) TRUE
let DECR = \n \rightarrow -- decrement n by one --
         = \a b -> -- return TRUE if a == b, otherwise FALSE --
let EQL
-- Recursion -----
let FIX = \langle x - \rangle (x - \rangle stp (x x)) (x - \rangle stp (x x))
```

2 Haskell cheat sheet

```
data Maybe a = Nothing | Just a
foldr :: (a -> b -> b) -> b -> [a] -> b
foldr f b [] = b
foldr f b (x:xs) = f x (foldr f b xs)
foldl :: (b -> a -> b) -> b -> [a] -> b
foldl f b xs
                      = helper b xs
  where
    helper acc [] = acc
    helper acc (x:xs) = helper (f acc x) xs
filter :: (a -> Bool) -> [a] -> [a]
filter p []
              = []
filter p (x:xs)
  | р х
               = x : filter p xs
                 = filter p xs
  otherwise
map :: (a -> b) -> [a] -> [b]
map []
          = []
map f (x:xs) = f x : map f xs
flip :: (a -> b -> c) -> b -> a -> c
flip f x y = f y x
(.) :: (b \rightarrow c) \rightarrow (a \rightarrow b) \rightarrow a \rightarrow c
(.) f g x = f (g x)
(++) :: [a] -> [a] -> [a]
(++) []
         ys = ys
(++) (x:xs) ys = x : xs ++ ys
class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool
class (Eq a) => Ord a where
  (<) :: a -> a -> Bool
  (<=) :: a -> a -> Bool
  (>) :: a -> a -> Bool
  (>=) :: a -> a -> Bool
  . . .
```