CSE 114A: Fall 2021

Foundations of Programming Languages

Monads

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Based on course materials developed by Nadia Polikarpova and Ranjit Jhala

Abstracting Code Patterns

Rendering the Values of a List

sqrList [] = []

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Abstracting Code Patterns

```
-- >>> showList [1, 2, 3]
-- ["1", "2", "3"]
showList :: [Int] -> [String]
showList [] = []
showList (n:ns) = show n : showList ns

Squaring the values of a list
-- >>> sqrList [1, 2, 3]
-- 1, 4, 9
sqrList :: [Int] -> [Int]
```

 $sqrList (n:ns) = n^2 : sqrList ns$

Common Pattern: map over a list

```
Refactor iteration into mapList
mapList :: (a -> b) -> [a] -> [b]
mapList f [] = []
mapList f (x:xs) = f x : mapList f xs

Reuse map to implement inc and sqr
showList xs = map (\n -> show n) xs

sqrList xs = map (\n -> n ^ 2) xs
```

What about trees?

```
data Tree a
  = Leaf
  | Node a (Tree a) (Tree a)
```

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What about trees?

```
-- >>> showTree (Node 2 (Node 1 Leaf Leaf) (Node 3 Leaf Leaf))
-- (Node "2" (Node "1" Leaf Leaf) (Node "3" Leaf Leaf))
showTree :: Tree Int -> Tree String
showTree (Leaf = ???
showTree (Node v 1 r) = ???

-- >>> sqrTree (Node 2 (Node 1 Leaf Leaf) (Node 3 Leaf Leaf))
-- (Node 4 (Node 1 Leaf Leaf) (Node 9 Leaf Leaf))
sqrTree :: Tree Int -> Tree Int
sqrTree Leaf = ???
sqrTree (Node v 1 r) = ???
```

QUIZ

Refactor iteration into mapTree! What should the type of mapTree be?

http://tiny.cc/cse116-maptree-ind

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QUIZ

Refactor iteration into mapTree! What should the type of mapTree be?

```
mapTree :: ???
showTree t = mapTree (\n -> show n) t
sqrTree t = mapTree (\n -> n ^ 2) t

(A) (Int -> Int) -> Tree Int -> Tree Int
(B) (Int -> String) -> Tree Int -> Tree String
(C) (Int -> a) -> Tree Int -> Tree a
(D) (a -> a) -> Tree a -> Tree a
(E) (a -> b) -> Tree a -> Tree b
```

http://tiny.cc/cse116-maptree-grp

Lets write mapTree

QUIZ

```
class Functor t where
  fmap :: ???

What type should we give to fmap?

(A) (b -> a) -> t b -> t a
(B) (a -> a) -> t a -> t a
(C) (a -> b) -> [a] -> [b]
(D) (a -> b) -> t a -> t b
(E) (a -> b) -> Tree a -> Tree b
```

http://tiny.cc/cse116-fmap-ind

QUIZ

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http://tiny.cc/cse116-fmap-grp
```

Reuse Iteration Across Types

```
instance Functor [] where
  fmap = mapList

instance Functor Tree where
  fmap = mapTree
And now we can do
-- >>> fmap (\n -> n^2) (Node 2 (Node 1 Leaf Leaf) (Node 3 Leaf Leaf))
-- (Node 4 (Node 1 Leaf Leaf) (Node 9 Leaf Leaf))
-- >>> fmap show [1,2,3]
-- ["1", "2", "3"]
```

Exercise: Write a Functor instance

Exercise: Write a Functor instance

Next: A Class for Sequencing

```
Recall our old Expr datatype

data Expr

= Number Int

| Plus Expr Expr
| Div Expr Expr
deriving (Show)

eval :: Expr -> Int
eval (Number n) = n
eval (Plus e1 e2) = eval e1 + eval e2
eval (Div e1 e2) = eval e1 `div` eval e2

-- >>> eval (Div (Number 6) (Number 2))
-- 3
```

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But, what is the result

```
-- >>> eval (Div (Number 6) (Number 0))
-- *** Exception: divide by zero
```

A crash! Lets look at an alternative approach to avoid dividing by zero.

The idea is to return a Result Int (instead of a plain Int)

- If a sub-expression had a divide by zero, return Error "..."
- If all sub-expressions were safe, then return the actual Result v

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But, what is the result

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But, what is the result

The good news, no nasty exceptions, just a plain Error result

```
\rightarrow eval (Div (Number 6) (Number 2))
Value 3
\rightarrow eval (Div (Number 6) (Number 0))
Error "yikes dbz:Number 0"
\rightarrow eval (Div (Number 6) (Plus (Number 2) (Number (-2))))
Error "yikes dbz:Plus (Number 2) (Number (-2))"
```

The bad news: the code is super duper gross

Let's spot a Pattern

The code is gross because we have these cascading blocks

- Value v -> {- do stuff with v -}

 1. Evaluate e
- 2. If the result is an Error then return that error.
- 3. If the result is a Value v then do some further processing on v.

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Let's spot a Pattern

Lets bottle that common structure in two functions:

- >>= (pronounced bind)
- return (pronounced return)

```
(>>=) :: Result a -> (a -> Result b) -> Result b
(Error err) >>= _ = Error err
(Ok v) >>= process = process v

return :: a -> Result a
return v = Ok v
```

NOTE: return is not a keyword; it is just the name of a function!

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A Cleaned up Evaluator

The magic bottle lets us clean up our eval

The gross pattern matching is all hidden inside >>=

A Cleaned up Evaluator

Notice the >>= takes *two* inputs of type:

- Result Int (e.g. eval e1 or eval e2)
- Int -> Result Int (e.g. The *processing* function that takes the v and does stuff with it)

In the above, the processing functions are written using

```
v1 \rightarrow \dots and v2 \rightarrow \dots
```

NOTE: It is *crucial* that you understand what the code above is doing, and why it is actually just a "shorter" version of the (gross) nested-case-of eval.

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A Class for >>=

Like fmap or show or jval or ==, the >>= operator is useful across many types, so we capture it in an interface/typeclass:

```
class Monad m where
  (>>=) :: m a -> (a -> m b) -> m b
  return :: a -> m a

Notice how the definitions for Result fit the above, with m = Result
instance Monad Result where
  (>>=) :: Result a -> (a -> Result b) -> Result b
```

(Error err) >>= _ = Error err (Ok v) >>= process = process v return :: a -> Result a return v = Ok v

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Syntax for >>=

In fact >>= is so useful there is special syntax for it.

Instead of writing

```
e1 >>= \v1 ->
e2 >>= \v2 ->
e3 >>= \v3 ->
e
you can write
do v1 <- e1
v2 <- e2
v3 <- e3
```

Syntax for >>=

Thus, we can further simplify our eval to:

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Purity and the Immutability Principle

Haskell is a **pure** language. Not a *value* judgment, but a precise *technical* statement:

The "Immutability Principle":

- A function must always return the same output for a given input
- A function's behavior should never change

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No Side Effects

Haskell's most radical idea: expression ==> value

 When you evaluate an expression you get a value and nothing else happens

Specifically, evaluation must not have any side effects

- change a global variable or
- print to screen or
- read a file or
- send an email or
- launch a missile.

Purity means functions may depend only on their inputs

functions should give the same output for the same input every time

But... how to write "Hello, world!"

But, we want to ...

- print to screen
- read a file
- send an email

A language that only lets you write factorial and fibonacci is ... not very useful!

Thankfully, you can do all the above via a very clever idea: Recipe

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Recipes

Haskell has a special type called **IO** - which you can think of as **Recipe**

type Recipe a = IO a

A value of type Recipe a is

- a description of an effectful computations
- when executed (possibly) perform some effectful I/O operations to
- produce a value of type a.

This analogy is due to Joachim Brietner

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Recipes have No Effects

A value of type Recipe a is

- Just a description of an effectful computation
- An inert, perfectly safe thing with no effects.

Merely having a Recipe Cake has no effects: holding the recipe

- Does not make your oven hot
- Does not make your your floor dirty

Executing Recipes

There is only one way to execute a Recipe a

Haskell looks for a special value

```
main :: Recipe ()
```

The value associated with main is handed to the runtime system and executed

The Haskell runtime is the only one allowed to cook!

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How to write an App in Haskell

Make a Recipe () that is handed off to the master chef main.

- main can be arbitrarily complicated
- will be composed of many smaller recipes

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Hello World

QUIZ: Combining Recipes

```
Next, lets write a program that prints multiple things:
main :: IO ()
main = combine (putStrLn "Hello,") (putStrLn "World!")

-- putStrLn :: String -> Recipe ()
-- combine :: ???
What must the type of combine be?

(A) combine :: () -> () -> ()
(B) combine :: Recipe () -> Recipe () -> Recipe ()
(C) combine :: Recipe a -> Recipe a -> Recipe a
(D) combine :: Recipe a -> Recipe b -> Recipe b
(E) combine :: Recipe a -> Recipe b -> Recipe a
```

Using Intermediate Results

Next, lets write a program that

```
    Asks for the user's name using getLine :: Recipe String
    Prints out a greeting with that name using putStrLn :: String -> Recipe ()
```

Problem: How to pass the **output** of *first* recipe into the *second* recipe?

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QUIZ: Using Yolks to Make Batter

```
Suppose you have two recipes

crack :: Recipe Yolk

eggBatter :: Yolk -> Recipe Batter

and we want to get

mkBatter :: Recipe Batter

mkBatter = crack `combineWithResult` eggBatter

What must the type of combineWithResult be?

(A) Yolk -> Batter -> Batter

(B) Recipe Yolk -> (Yolk -> Recipe Batter) -> Recipe Batter

(C) Recipe a -> (a -> Recipe a ) -> Recipe a

(D) Recipe a -> (a -> Recipe b ) -> Recipe b

(E) Recipe Yolk -> (Yolk -> Recipe Batter) -> Recipe ()
```

Look Familiar?

```
Wait a bit, the signature looks familiar!

combineWithResult :: Recipe a -> (a -> Recipe b) -> Recipe b

Remember this?

(>>=) :: Result a -> (a -> Result b) -> Result b
```

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Recipe is an instance of Monad

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Recipe is an instance of Monad

Exercise

- 1. Compile and run to make sure its ok!
- 2. Modify the above to repeatedly ask for names.
- 3. Extend the above to print a "prompt" that tells you how many iterations have occurred.

Monads are Amazing

Monads have had a $\it revolution ary$ influence in PL, well beyond Haskell, some recent examples

- Error handling in go e.g. 1 and 2
- Asynchrony in JavaScript e.g. 1 and 2
- Big data pipelines e.g. LinQ and TensorFlow
- and Language-based security!